

Note that it's very unusual that the randomly generated private key is only 128 bits instead of the full 384 bits available! We'll see how this helps later.

Let's check what the order of the generator is using SageMath:

Python

```
sage: p =
0xc90102faa48f18b5eac1f76bb40a1b9fb0d841712bbe3e5576a7a56976c2baeca47809765283aa078583e1e6517
2a3fd
....: a =
0xa079db08ea2470350c182487b50f7707dd46a58a1d160ff79297dcc9bfad6fcf96a81c4a97564118a40331fe0fc
1327f
....: b =
0x9f939c02a7bd7fc263a4cce416f4c575f28d0c1315c4f0c282fca6709a5f9f7f9c251c9eede9eb1baa31602167f
a5380
....: gx =
0x087b5fe3ae6dcfb0e074b40f6208c8f6de4f4f0679d6933796d3b9bd659704fb85452f041fff14cf0e9aa7e4554
4f9d8
....: gy =
0x127425c1d330ed537663e87459eaa1b1b53edfe305f6a79b184b3180033aab190eb9aa003e02e9dbf6d593c5e3b
08182
....: E = EllipticCurve(Zmod(p), [a,b])
....: gen = E(gx,gy)
....: factor(gen.order())
35809 * 46027 * 56369 * 57301 * 65063 * 111659 * 113111 *
7072010737074051173701300310820071551428959987622994965153676442076542799542912293
```

The order is almost smooth! If it were smooth, then we could use [Pohlig-Hellman](#) to recover the private key, but unfortunately we still have a large prime factor in the order. However, we can still apply Pohlig-Hellman partially to gain information about the private key:

Recall that Pohlig-Hellman does the following (using multiplicative group notation):

- Given: generator g in a group of order n , element $h = \text{secret} \cdot g$ where $\text{secret} < n$ is secret.
- For each prime (power) p in the factorization of the order:
 - Compute $g_2 = (n/p) \cdot g$, $h_2 = (n/p) \cdot g$.
 - Solve the discrete logarithm problem using g_2 as the generator and h_2 . This subgroup has order p .
 - The solution to the discrete logarithm problem is secret modulo p .
- Combine all the values for secret modulo p using the [Chinese remainder theorem](#) to recover secret .

We can apply these steps to the small prime factors of the order to get the private key modulo the product of those factors! If the product was larger than the private key, then this would just be the private key and we would be done. Unfortunately, we still come up short: the product is only 112 bits, not the full 128 bits we need.


```

ax = unpack(raw[48*0:48*1]) ^ xorkey
ay = unpack(raw[48*1:48*2]) ^ xorkey
bx = unpack(raw[48*2:48*3]) ^ xorkey
by = unpack(raw[48*3:48*4]) ^ xorkey
raw = raw[48*4:]
A = E(ax, ay)
B = E(bx, by)

print('calculating order...')
order = gen.order()
print(f'{order}')
factors = factor(order, proof=False)
smooth_part = Factorization(factors[:-1]).value()
big_part = Factorization(factors[-1:]).value()

# apply pohlig-hellman partially by dividing out the big factor
secret_mod_smooth = (gen*big_part).discrete_log(A*big_part)
print(f'{secret_mod_smooth}')

possible_secret = secret_mod_smooth
while True:
    AB = possible_secret * B
    h = hashlib.sha512(int(AB[0]).to_bytes(48, 'big')).digest()
    key = h[:32]
    iv = h[32:40]
    cipher = ChaCha20.new(key=key, nonce=iv)
    test = cipher.decrypt(raw[:6])
    if test == b'verify':
        print('secret found:', possible_secret)
        cipher.seek(0)
        lines = cipher.decrypt(raw).decode().strip('\x00').split('\x00')
        print(lines)
        print(base64.b64decode(lines[-2]))
        break
    possible_secret += smooth_part

```

Solution script output:

Unset

```

calculating order...
order=309373396510199458922447942662567138904409224558720519847625055617635267803116168639895
11376879697740787911484829297

```

```
secret_mod_smooth=3914004671535485983675163411331184
secret found: 168606034648973740214207039875253762473
['verify', 'verify', 'ls', '==== dirs ====\r\nsecrets\r\n==== files ====\r\nfullspeed.exe\r\n', 'cd|secrets', 'ok', 'ls', '==== dirs ====\r\nsuper secrets\r\n==== files ====\r\n', 'cd|super secrets', 'ok', 'ls', '==== dirs ====\r\n.hidden\r\n==== files ====\r\n', 'cd|.hidden', 'ok', 'ls', "==== dirs ====\r\nnwait, dot folders aren't hidden on windows\r\n==== files ====\r\n", "cd|wait, dot folders aren't hidden on windows", 'ok', 'ls', '==== dirs ====\r\n==== files ====\r\nflag.txt\r\n', 'cat|flag.txt', 'RDBudF9VNWVfeTB1cl9Pd25fQ3VSdjNzQGZsYXJ1LW9uLmNvbQ==', 'exit']
b'D0nt_U5e_y0ur_Own_CuRv3s@flare-on.com'
```

Final Flag

Unset

D0nt_U5e_y0ur_Own_CuRv3s@flare-on.com